

538.9

$$D = (-1 < x < 1, y < 0)$$

$$u(x, y)$$

$$u(x, y)$$

$$u_{xx} + u_{yy} + \omega u_y = 0, (x, y) \in D, \quad (1)$$

$$u_x \pm \omega_0 u = 0, x = \pm 1, \tag{2}$$

$$u(x, -\infty) = 0, \tag{3}$$

$$u_y(x, 0) = v(x), -1 \leq x \leq 1. \tag{4}$$

$$\omega = \omega_0 - \dots, \tag{1} \tag{4}$$

$$u(x, y) = \sum_{n=0}^{\infty} \frac{\cos \lambda_n x e^{\mu_n y}}{\mu_n \left(1 + \omega_0 \frac{\cos^2 \lambda_n}{\lambda_n^2}\right)^{-1}} \int_{-1}^1 v(\xi) \cos \lambda_n \xi d\xi, \tag{5}$$

$$\mu_n = -\frac{\omega}{2} + \sqrt{\frac{\omega^2}{4} + \lambda_n^2}, n = 1, 2, 3, \dots, \lambda_n -$$

$$\lambda = \omega_0 \operatorname{ctg} \lambda.$$

$$u(x, y)$$

W_1, W_2 и W_3 ,

$$\{ -1 \leq x \leq 1, y = 0 \},$$

$x = \pm 1$.

T^* ,

(2).

$$(5) v(x) = (W_1, W_2, W_3).$$

$$I(v) = \int_{-1}^1 (u(1, y) - T^*)^2 dx. \tag{6}$$

U ,

$v(x)$

$I(v)$.

$$v_{n+1} = v_n + \varepsilon_n (v_{n-1} - v_n),$$

v_n
 ε_n

$$\min_{0 \leq \varepsilon_n \leq 1} I(v_n + \varepsilon_n (v_{n-1} - v_n)).$$

U

$$v = v_k, x_k \leq x \leq x_{k+1}, v_k = \text{const}, k = 0, 1, 2, \dots, m.$$

(5)

$$u(x, y) = \sum_{n=0}^{\infty} \frac{\cos \lambda_n x e^{\mu_n y}}{\mu_n \left(1 + \omega_0 \frac{\cos^2 \lambda_n}{\lambda_n^2}\right)} \sum_{k=0}^{\infty} v_k \frac{\sin \lambda_n x_{k+1} - \sin \lambda_n x_k}{\lambda_n},$$

$$I(v) = I(v_0, v_1, v_2, \dots, v_m).$$

