# FAULT DIAGNOSIS OF INDUCTION MOTOR USING NEURAL NETWORKS

QING HE, DONG-MEI DU

Key Laboratory of Condition Monitoring and Control for Power Plant Equipment, Ministry of Education, College of Energy and Power Engineering, North China Electric Power University, Beijing 102206, China E-MAIL: hqng@163.com, ddongm@ncepu.edu.cn

## Abstract:

The fault diagnosis theory and its methods for inductor motor are summarized. Based on the method of current spectrum, a neural network method to diagnose the broken bar number of inductor motor is presented. The training patterns and the diagnosis results for the neural network are given. The broken bar number of inductor motor is diagnosed directly according to the working status parameters. The method is high intelligent and very reliable.

#### **Keywords:**

Induction motor; Broken bar; Neural networks; Fault diagnosis

## 1. Introduction

The fault analysis and diagnosis of the electric motor are very important in equipment diagnosis technique. Because of the work principle and structure characteristics of electric motor, the diagnosis methods and techniques have many characteristics <sup>[1]</sup>. A fault of electric motor usually has many symptoms, for example, when a bar of squirrel cage induction motor is broken, many symptoms associated each other occur, such as vibration increment, starting time prolongation, stator current swing, slip enlargement, speed and torque undulation, temperature change, and so on. After one bar broken, if electric motor continues to run, the number of broken bar will easily increase, symptoms be more and more obvious, fault become more and more serious, and finally electric motor will be damaged.

On the other hand, many faults cause same symptoms. Many situation changes may cause electric motor fault, for example, load, condition and other operation etc, which all kinds of symptoms occur and the relation is very complicated. Therefore, it is very difficult to diagnose the faults of electric motor. For long time, many diagnosis techniques and methods have been obtained by a great deal of research work, such as current analysis, vibration diagnosis, temperature diagnosis, and so on. Some expert systems for fault diagnosis of electric motor have been developed<sup>[1-5]</sup>.

Currently, research on fault analysis and diagnosis system is still a significant problem because (a) the relation between fault reason and symptom is very complex; (b) the capability of fault diagnosis system of motor is very limited; (c) for the artificial intelligence diagnosis system based on rule discursion, there are many problems such as knowledge obtaining and expression, rule match, and so on.

The principle and method of fault diagnosis of squirrel cage induction motor is discussed. On the basis of the analysis method of current spectrum, a diagnosis method based on neural network for the number of broken bar of induction motor is presented. From the condition parameters of motor, the method can directly identify the number of broken bar. This method is exact, reliable and intelligent in diagnosis.

# 2. Fault diagnosis theory of broken bar

The stator current frequency of the good induction motor is single, i.e. supply frequency. While rotor circuit has a fault, there are two side frequencies  $(\pm 2sf)$  in the stator current spectrum. The magnetomotive force of stator winding of induction motor is

$$m_1 = K_1 N_1 I_1 \sin[(\omega_0 - \omega_r)t - \phi]$$
(1)

where  $K_1$  is a stator constant related to pole-pair number and winding coefficient;  $N_1$  is the stator winding number per phase;  $I_1$  is stator current,  $\omega$  is the angular frequency of power,  $\omega=2\pi f$ , f is current frequency,  $\phi$  is the phase angle of rotor winding,  $\phi=\theta-\omega_{e}t$ ,  $\theta$  is the initial phase angle,  $\omega_{e}$  is the rotating angular velocity of rotor.

When rotor circuit has a fault, the magnetomotive force of rotor winding is modulated by  $\sin 2\phi$ . So the magnetomotive force of rotor winding becomes

$$m_1 = \frac{K_2 N_2 I_2}{2} \{ \cos[(3-2s)\omega t - 3\theta] - \cos[(1-2s)\omega t - \theta] \} (2)$$

where s is slip,  $s = (\omega - \omega_r)/\omega$ ,  $K_1$  is a rotor constant related to pole-pair number and winding coefficient,  $N_1$  is the rotor

# 1-4244-0973-X/07/\$25.00 ©2007 IEEE

winding number per phase;  $I_1$  is rotor current.

The first item in equation (2) has  $3\omega t$  and  $3\theta$ , which will produce zero sequence magnetomotive force in threephase stator winding and has no influence on the power supply current. The second item has a component  $2s\omega$  less than supply frequency and makes stator winding produce three-phase current component  $2s\omega$  less than supply frequency, which modulation makes stator current beat vary (beat wave) and rotor speed wave with two-time slip frequency. Speed wave reduces low-side frequency  $\omega(1-2s)$ and current swing scope and produces up-side frequency  $\omega(1+2s)$  and is increased by three-harmonic magnetic flux in modulation. Thus, the amplitude ratio of low-side frequency to supply frequency can directly reflect the damage degree of rotor.

Broken bar of squirrel cage motor brings unbalanced electromagnetic force that rotates around rotor and makes motor electromagnetic vibration. When the load increases, vibration also increases. The pulse wave with frequency 2sf occurs in stator current, which causes the side frequencies  $\pm 2sf$  at supply frequency in current spectrum. Therefore, the amplitudes of side frequencies  $\pm 2sf$  in current spectrum can be used to diagnose the number of broken bar. This is basic principle that the number of broken bar is diagnosed by the stator current spectrum of squirrel cage motor.

## 3. Fault diagnosis principle of current analysis

In normal running, the stator current of electrical motor has only supply frequency in theory. When there are faults in the rotor, additional side frequency (1-2s)f occurs in stator current which amplitude is related mainly to rotor asymmetrical degree. It is possible to diagnose rotor faults by detecting amplitude of additional side frequency (1-2s)f in stator current.

According to the principle of diagnosing broken bar by the stator current spectrum of induction motor, the fault strictness factor *SF* is defined as following:

$$SF = \frac{P(f - 2sf) + P(f + 2sf)}{P(f)}$$
 (3)

where P(f) is the spectrum amplitude at supply frequency;  $P(f\pm 2sf)$  is the spectrum amplitude at side frequencies.

The *SF* is not same for different electrical motor and running condition. The relation of *SF* vs. rotor broken bar ratio and load is shown in Figure.1.

Figure 1 shows that the factor SF is not only related to number of rotor broken bar, but also to operating parameters such as load<sup>[1,3]</sup> etc. Thus, it is not available to determine motor condition only in accordance with the value of SF when diagnosing. Figure 2 shows the relation



Figure 1. *SF* vs ratio of broken bar to load (0dB as the amplitude of base harmonic)



Figure 2. Amplitude difference of current spectrum vs load current when one broken bar

between the amplitude difference of current spectrum and load current when one broken bar occurs.

#### 4. Diagnosing broken bar using neural networks

The fault of broken bar brings side frequency component (1-2s)f in current of stator winding. The amplitude of side frequency is relative to many factors. Thus, it is very difficult to diagnose the number of broken bars only using amplitude of side frequency component, which is relative to broken bar number and other operating parameters. This complex nonlinear relation can be mapped by artificial neural networks.

## 4.1. BP networks

To diagnose the number of broken bars of motor rotor is an essentially classification problem in pattern space. The Back-Propagation (BP) networks are simple in structure

and stable in operation. The BP networks have been successfully used for many applications, such as pattern recognition, nonlinear mapping, and so on. The BP networks including hide layers are capable of classification of arbitrary region of multidimensional space (i.e., for any mapping *G* from [0,1] to *R* in an arbitrary set *L*, there is a three-layer BP network that can approach to *G* in any way.) <sup>[20]</sup>. Thus, a three-layer BP networks are used to diagnose the number of broken bar.

For a three-layer BP networks shown as in Figure.3, given the input layer node number n, the output layer node number m, the hidden layer node number l, pattern number N, the input vector  $(x_1, x_2, ..., x_n)$ , the weight between input layer node and hidden layer node is  $w_{ji}$ , the input  $NET_j$  and output  $O_j$  of hidden layer node input are

$$NET_{j} = \sum_{i=1}^{n} (x_{i} * w_{ji})$$
(4)

$$O_j = f(NET_j) \tag{5}$$

Generally, node activation function uses sigmoid function as

$$f(x) = \frac{1}{1 + e^{-x}} \tag{6}$$

Suppose the connecting weight between output layer node k and hidden layer node j is  $w_{kj}$ , the node output of output layer k is

$$y_k = f(\sum_{j=1}^{l} (w_{kj} * O_j))$$
(7)

The square error function is used. For all pattern, the total error is

$$E = \frac{1}{2} \sum_{p=1}^{N} \sum_{k=1}^{m} (y_{kp} - \hat{y}_{kp})^2$$
(8)

where  $y_{kp}$  is the actual output of the nerve cell k at output layer for the pattern p;  $\hat{y}_{kp}$  is the target output of the pattern p.



Figure 3. A three-layer BP networks

The BP algorithm is the grads descend method of nonlinear optimization algorithm. The learning algorithm of the BP networks is actually a batch learning method.

It is complicated to determine the node number of hidden layer of the BP networks. If the node number of hidden layer is too small, the network may not be trained or not strong, whereas, if the node number of hidden layer is too large, the training time may be too long and the error may not be the smallest. Therefore, there is a best node number of hidden layer. Generally, the node number of hidden layer  $n_1$  can be given as following equation<sup>[6]</sup>

$$n_1 = \sqrt{n+m+a} \tag{9}$$

where n is the node number of input layer, m is the node number of output layer, a is a constant in the range 1-10.

## 4.2. BP networks for diagnosis of broken bar

Fault diagnosis is the pattern classification. The BP networks can sort input pattern space by nonlinear mapping and be applied extensively in pattern recognition and classification. It is a nonlinear function-mapping problem to diagnose the number of broken bar of motor rotor by amplitude of side frequency of current spectrum. Therefore, the BP networks can be used to diagnose the number of broken bar. A three-layer BP networks can approach the nonlinear function between the number of broken bar and the amplitude of current spectrum of motor as well as the other operation condition parameters.

#### 4.2.1. Output layer

The output of BP networks must correspond to the number of broken bar. Generally, the number of rotor bar of large-scale and medium-scale squirrel cage motor is about 100. So assume the maximum number of broken bar  $N_m$ =100. The factor of broken bar number as output of BP networks is defined as

$$y=10(n+1)/N_m$$
 (10)

where *n* is the number of broken bar.

If no broken bar, i.e. n=0, the BP network output y=0.1. If the number of broken bar is one, the BP network output y=0.2. So, the BP network output corresponds one-to-one to the number of broken bar.

According to the output of neural networks and equation (10), the broken bar number can be calculated as following

$$n_b = \text{INT}(yN_m/10-0.5)$$
 (11)

where  $n_b$  is the broken bar number; y is the output value of networks (broken bar factor); INT is integer conversion.

#### 4.2.2. Input layer

The normalized parameters of current spectrum components and working conditions are selected as the input nodes of neural network as following

$$x_1 = s \tag{12}$$

where *s* is the practice slip.

$$x_2 = s/s_r \tag{13}$$

where  $x_2$  is the slip referred to the rated one;  $s_r$  is the rated slip.

$$x_3 = 20 \lg(I_0/I^*) / 100 \tag{14}$$

where  $x_3$  is the amplitude level of current spectrum;  $I^*$  is the spectrum amplitude at the left side frequency;  $I_0$  is the spectrum amplitude at the power frequency.

$$x_4 = N/N_m \tag{15}$$

where N is the total bar;  $N_m$  is the maximum bar,  $N_m$ =100.

$$x_5 = I/I_r \tag{16}$$

where  $x_5$  is the current referred to  $I_r$ ; I is the practice load current;  $I_r$  is the rated current.

$$x_6 = P_r / P_b \tag{17}$$

where  $x_6$  is the rated power referred to  $P_b$ ;  $P_r$  is the rated power;  $P_b$  is the maximum power,  $P_b=2000$ kW.

## 4.2.3. Hidden layer

According to equation (9), the node number of hidden layer should be in  $3\sim13$ . In order to increase the generalized ability of BP networks, the node number of hidden layer



Figure 4. BP networks diagnosing broken bar number

 $n_1$ =15. Figure 4 is the BP networks for diagnosing broken bar number.

## 4.3. Learning and test

According to the data shown in Table 1 from [1], the BP networks patterns shown in Table 2 are obtained. The first eight patterns are used to train the networks, and the last three patterns are used to test the networks. The training and test results are shown in Table 2 and Table 3. Error control value for training is given  $\varepsilon$ =0.00001. The training iteration is shown in Figure 5. From Table 2, the absolute errors between the network outputs and the object outputs for all training patterns are less than 0.015 after 18671 iterations. The diagnosis results of three test patterns in Table 3 are completely correct. It is shown that the BP networks have the very high diagnosis accuracy and good generalized ability.

# 5. Conclusions

The principle and methods of fault diagnosis for induction motor have been analyzed. Based on the current spectrum analysis, the neural networks method to diagnose the number of broken bar has been presented. The structure of neural networks, training patterns, and as well as the results of training and testing has been given. It is proved that this method can exactly diagnose the number of broken bar according to condition parameters.

Table 1. Broken bar number vs condition parameters

	No	Broken bar number	Rated voltage (V)	Rated current (A)	Load current (A)	Speed (rpm)	Power frequency component(dB)	Side frequency (dB)	Spectrum difference (dB)
	1	0	380	21.8	21.8	1430	115.6	51.6	64.0
	2	1	380	21.8	21.8	1430	115.6	71.0	44.6
	3	2	380	21.8	21.8	1430	115.6	78.4	37.2
	4	3	380	15.1	15.1	1450	49.3	28.4	20.9
	5	1	380	21.8	24.2	1420	116.4	72.0	44.4
	6	1	380	21.8	19.5	1440	114.7	69.0	45.7
	7	1	380	21.8	17.4	1450	113.7	66.0	47.7
	8	1	380	21.8	15.8	1460	112.8	63.9	48.9
	9	1	380	21.8	14.5	1470	111.9	60.5	51.4
	10	1	380	21.8	13.4	1480	110.2	56.7	53.5
	11	1	380	21.8	13.0	1490	110.9	49.6	61.3

Ma			У					
INO	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	Desired	Output
1	0.047	1.000	0.640	0.51	1.000	0.012	0.1	0.101
2	0.047	1.000	0.446	0.51	1.000	0.012	0.2	0.215
3	0.047	1.000	0.372	0.51	1.000	0.012	0.3	0.303
4	0.033	1.000	0.209	0.26	1.000	0.009	0.4	0.412
5	0.053	1.143	0.444	0.51	1.110	0.012	0.2	0.211
6	0.040	0.857	0.457	0.51	0.895	0.012	0.2	0.213
7	0.027	0.571	0.489	0.51	0.725	0.012	0.2	0.209
8	0.013	0.258	0.535	0.51	0.615	0.012	0.2	0.208

Table 2. Learning patterns

- 1		•	-		
Tal	ble.	3	Test	natterns	1

No			Broken bar number					
	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	Actual	$n_b(y)$
1	0.033	0.714	0.477	0.51	0.798	0.012	1	1(0.195)
2	0.020	0.428	0.514	0.51	0.665	0.012	1	1(0.205)
3	0.013	0.286	0.613	0.51	0.596	0.012	1	1(0.181)



Figure 5. Training Iteration of BP networks

## References

- [1] Sheng B. Z., Electric motor fault diagnosis technique, Machinery industry press, Beijing, 1996.
- [2] Filiooetti F., Franceschini G., Tassoni C., Neural networks aided on-line diagnostics of induction motor
- [3] rotor faults, IEEE trans. IA, Vol.31, No.4, 1995, 892-899.
- [4] Walliser R. F., Landy C. F., Determination of interbar current effects in the detection of broken rotor bars in squirrel cage induction motors, IEEE trans. EC, Vol.9, No.1, 1994, 152-158.

- [5] Chow M., Yee S. O., Methodology for on-line incipient fault detection in single-phase squirrel-cage induction motors using artificial neural networks, IEEE trans. EC, Vol.6, No.3, 1991, 536-545.
- [6] Rafimanzelat M. R., Araabi B. N., Khosroshahli E., Induction machine broken bar detection using neural networks based classification. 2004 IEEE Conference on cybernetics and intelligent systems, 2004, p.1361-1366.
- [7] Cupertino F.; De V. E., Forcella G., Salvatore L., Stasi, S., Detection of IM broken rotor bars using MUSIC pseudo-spectrum and pattern recognition, IECON Proceedings (Industrial Electronics Conference), v.3, 2003, p.2829-2834.
- [8] Siau J. M. B., Graff A. L., Soong W. L., Ertugrul N. Broken bar detection in induction motors using current and flux spectral analysis, Australian journal of electrical and electronics engineering, v.1, n.3, 2004, p.171-177.
- [9] Li L. X., Mechefske C. K., Li W. D., Electric motor faults diagnosis using artificial neural networks, Insight: Non-destructive testing and condition monitoring, v.46, n.10, 2004, p.616-621.
- [10] Huang D, Huang C. L., Motor fault diagnosis expert system based on neural network, Automatic instrument, 2003(3).
- [11] Elkasabgy N. M., Eastham A. R., Dawson G. E., Detection of broken bars in the cage rotor on an induction machine, IEEE Transactions on industry applications, vol.28, no.1, 1992, pp.165-170.
- [12] Natarajan R. Failure Identification of induction motors by sensing unbalanced stator currents, IEEE Transactions on energy conversion, vol.4, no.4, 1989, pp.585-590.
- [13] Chow M. Y., Mangum P. M., Yee S. O., A neural network approach to real-time condition monitoring of induction motors, IEEE Transactions on industrial electronics, vol.38, no.6, 1991, pp. 448-453.
- [14] Schoen R. R., Habetler T. G., Effects of time-varying loads on rotor fault detection in induction machines, IEEE Transactions on Industry Applications, vol.31, no.4, 1995, pp.900-906.
- [15] Schoem R. R., Lin B. K., Habetler T. G., Schlag J. H. An unsupervised, on-line system for induction motor fault detection using stator current monitoring, IEEE Transactions on industry application, vol.31, no.6, 1995, pp.1280-1286.
- [16] Tallam R. M., Habetler T. G., Harley R. G., Continual on-line training of neural networks with applications to electric machine fault diagnostics, Power electronics specialists conference, IEEE 32nd Annual, vol.4, 2001, pp.2224-2228.

- [17] Nandi, S. Toliyat H. A., Condition monitoring and fault diagnosis of electrical machines-a review, Industry applications conference, IEEE thirty-fourth IAS annual meeting, vol.1, 1999, pp.197-204.
- [18] Filippetti F., Franceschini G., Tassoni C., Vas P., Recent developments of induction motor drives fault diagnosis using AI techniques, IEEE Transactions on industrial electronics, vol.47, 2000, pp.994-1004.
- [19] Demian C., Cirrincione G., Capolino G. A. A neural approach for the fault diagnostics in induction machines, IEEE 2002 28th annual conference of the

industrial electronics society, vol.4, 2002, pp.3372-3376.

- [20] Siddique A., Yadava G. S., Singh B., Applications of artificial intelligence techniques for induction machine stator fault diagnostics: review, diagnostics for electric machines, Power electronics and drives, 4th IEEE International symposium, 2003, pp.29-34.
- [21] Zhang L. M., Model and application of artificial neural networks, Fudan university press, Shanghai, 1993.